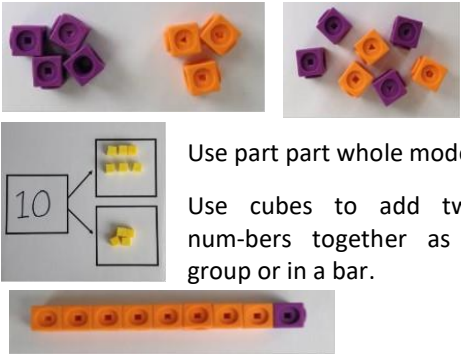
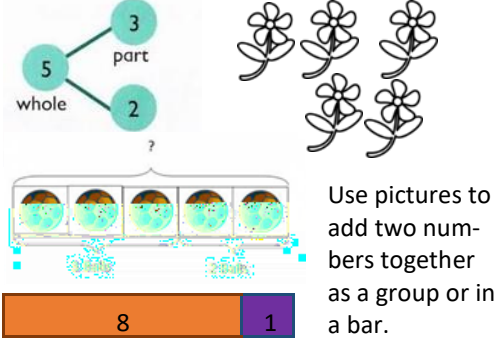
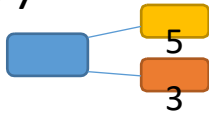

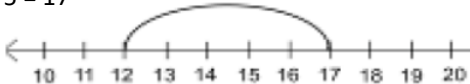
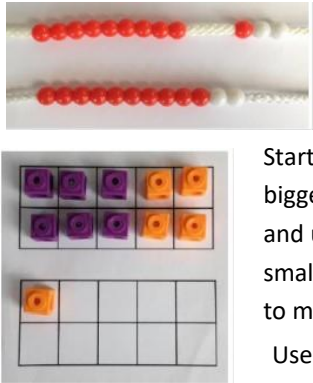
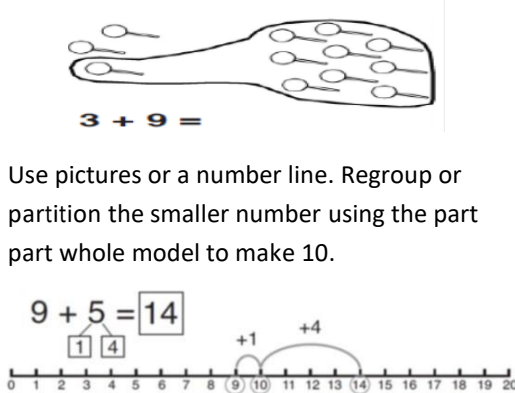

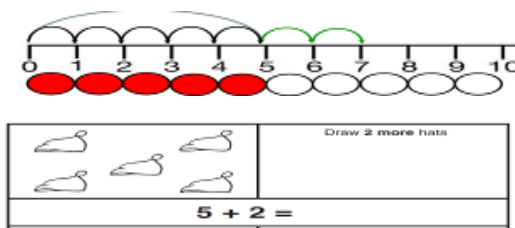


Mathematics Calculation Policy

Adapted from White Rose.

Mathematics at The Willows


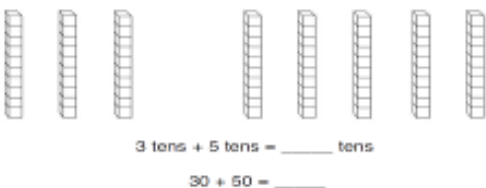
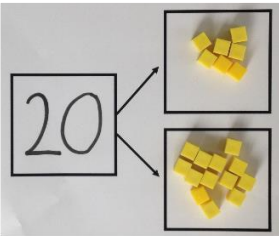
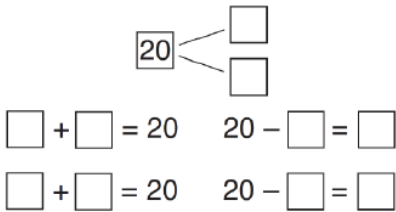
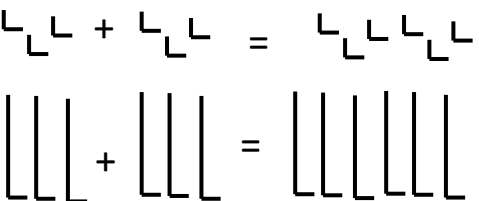
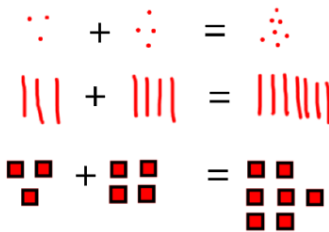


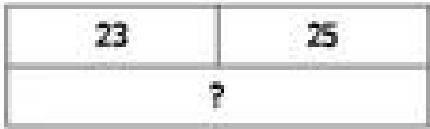
Mathematics is a creative and highly inter-connected discipline essential to everyday life. A high-quality mathematics education provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject' - National Curriculum, 2014

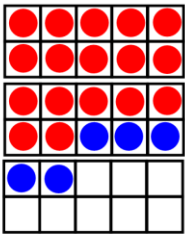
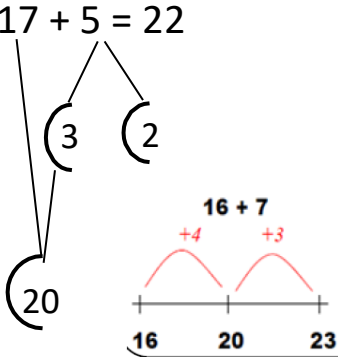
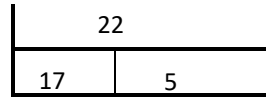

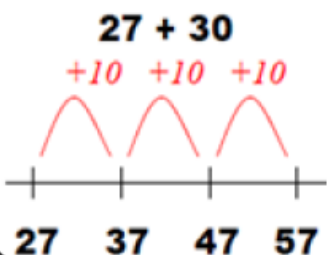
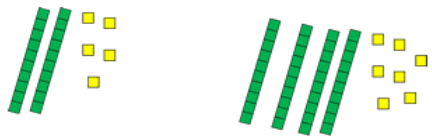
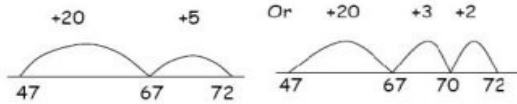
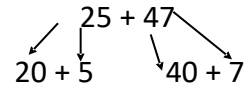
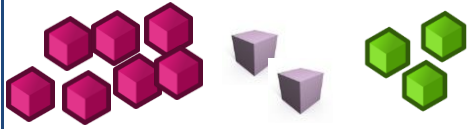
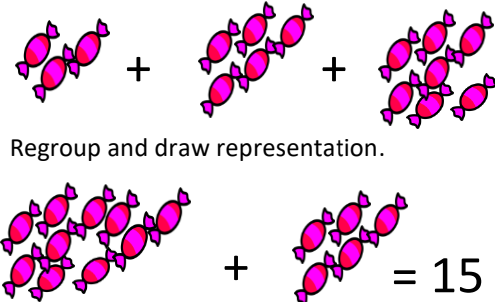
Objective & Strategy	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	 <p>Use part part whole model.</p> <p>Use cubes to add two num-bers together as a group or in a bar.</p>	 <p>Use pictures to add two num-bers together as a group or in a bar.</p>	<p>$4 + 3 = 7$</p>  <p>Use the part-part whole diagram as shown above to move into the abstract.</p> <p>$10 = 6 + 4$</p>
Starting at the bigger number and counting on	 <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p>	<p>$12 + 5 = 17$</p>  <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p>	<p>$5 + 12 = 17$</p> <p>Place the larger number in your head and count on the smaller number to find your answer.</p>
Regrouping to make 10. <i>This is an essential skill for column addition later.</i>	 <p>$6 + 5 = 11$</p> <p>Start with the bigger number and use the smaller number to make 10.</p> <p>Use ten frames.</p>	 <p>Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10.</p>	<p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p>
Represent & use number bonds and related subtraction facts within 20	 <p>2 more than 5.</p>	 <p>$5 + 2 =$</p>	<p>Emphasis should be on the language</p> <p>'1 more than 5 is equal to 6.'</p> <p>'2 more than 5 is 7.'</p> <p>'8 is 3 more than 5.'</p>

Y1

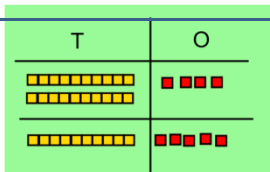
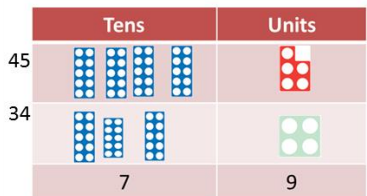
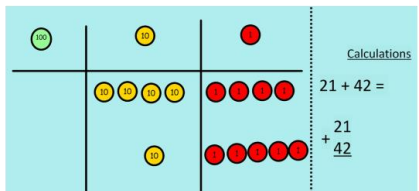
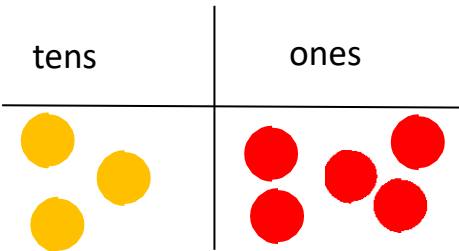
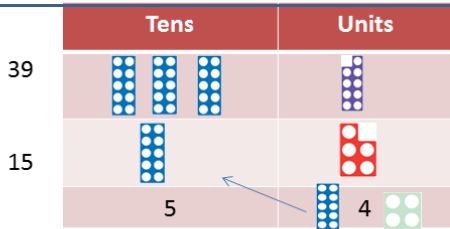
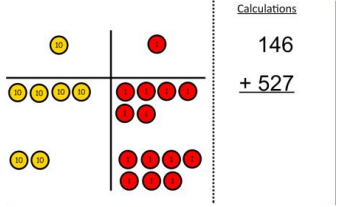
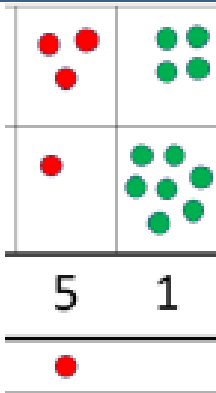
ADDITION +

Y2 ADDITION +

Objective & Strategy	Concrete	Pictorial	Abstract
Adding multiples of ten	$50 = 30 + 20$  Model using dienes and bead strings	 $3 \text{ tens} + 5 \text{ tens} = \underline{\hspace{2cm}} \text{ tens}$ $30 + 50 = \underline{\hspace{2cm}}$ Use representations for base ten.	$20 + 30 = 50$ $70 = 50 + 20$ $40 + \square = 60$
Use known number facts Part part whole	 Children explore ways of making numbers within 20	 $\square + \square = 20$ $20 - \square = \square$ $\square + \square = 20$ $20 - \square = \square$	$\square + 1 = 16$ $16 - 1 = \square$ $1 + \square = 16$ $16 - \square = 1$
Using known facts		 Children draw representations of H,T and O	$3 + 4 = 7$ <i>leads to</i> $30 + 40 = 70$ <i>leads to</i> $300 + 400 = 700$
Bar model	 $3 + 4 = 7$	 $7 + 3 = 10$	 $23 + 25 = 48$













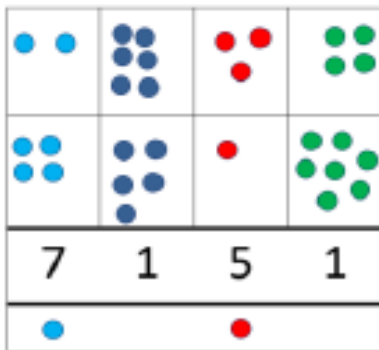
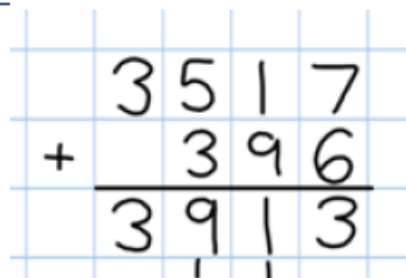












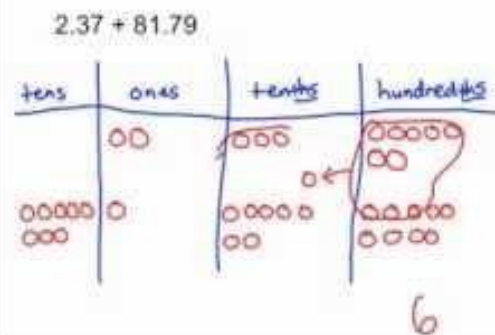
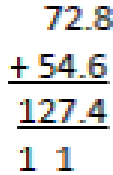
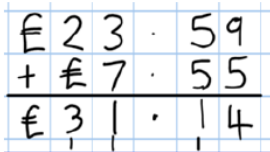



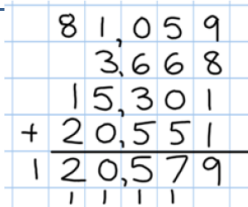
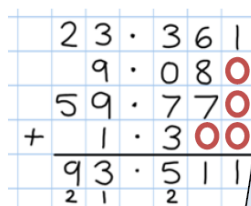
Objective & Strategy	Concrete	Pictorial	Abstract
Add a two digit number and ones	 <p> $17 + 5 = 22$ Use ten frame to make 'magic ten' </p> <p>Children explore the pattern.</p> <p> $17 + 5 = 22$ $27 + 5 = 32$ </p>	<p>Use part part whole and number line to model.</p> <p> $17 + 5 = 22$ </p> 	<p> $17 + 5 = 22$ </p> <p>Explore related facts</p> <p> $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$ </p> 
Add a 2 digit number and tens	 <p> $25 + 10 = 35$ Explore that the ones digit does not change </p>	<p> $27 + 30$ </p> 	<p> $27 + 10 = 37$ $27 + 20 = 47$ $27 + \square = 57$ </p>
Add two 2-digit numbers	 <p>Model using dienes, place value counters and numicon</p>	 <p>Use number line and bridge ten using part whole if necessary.</p>	<p> $25 + 47$ </p>  <p> $20 + 40 = 60$ $5 + 7 = 12$ $60 + 12 = 72$ </p>
Add three 1-digit numbers	 <p>Combine to make 10 first if possible, or bridge 10 then add third digit</p>	 <p>Regroup and draw representation.</p> <p> $4 + 7 + 6 = 17$ </p>	<p> $4 + 7 + 6 = 10 + 7$ $= 17$ </p> <p>Combine the two numbers that make/ bridge ten then add on the third.</p>

Y3 ADDITION +

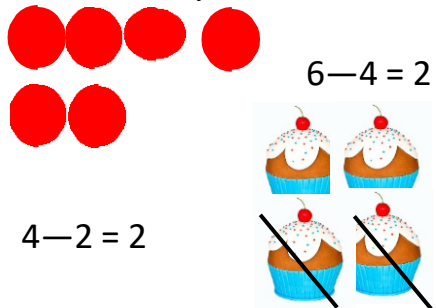
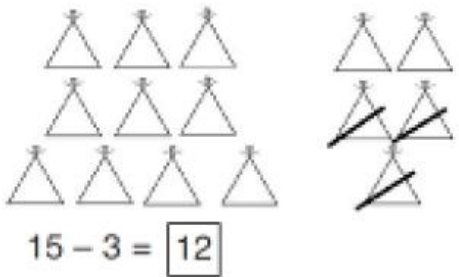
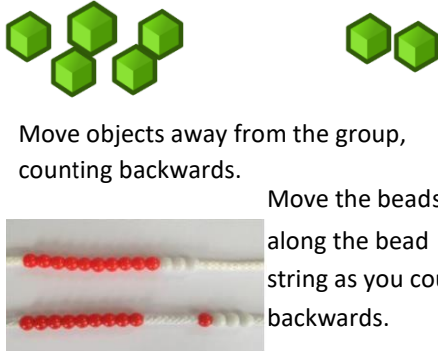
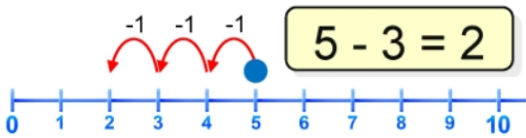
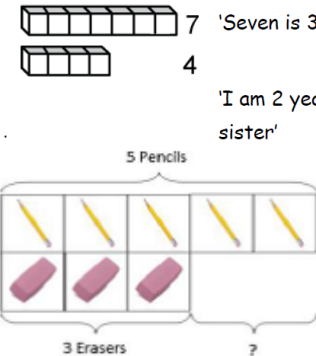
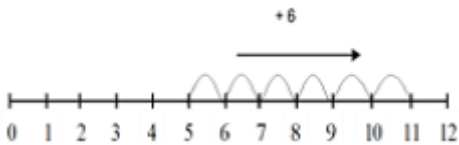
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Column Addition—no regrouping (friendly numbers)</p> <p>Add two or three 2 or 3-digit numbers.</p>	<p>Model using Dienes or numicon</p>  <p>Add together the ones first, then the tens.</p>   <p>Move to using place value counters</p>	<p>Children move to drawing the counters using a tens and one frame.</p> 	$\begin{array}{r} 223 \\ + 114 \\ \hline 337 \end{array}$ <p>Add the ones first, then the tens, then the hundreds.</p>
<p>Column Addition with regrouping.</p>	 <p>Exchange ten ones for a ten. Model using numicon and pv counters.</p> 	 <p>Children can draw a representation of the grid to further support their understanding, carrying the ten <u>underneath</u> the line</p>	$\begin{array}{r} 20 + 5 \\ 40 + 8 \\ 60 + 13 = 73 \end{array}$ <p>Start by partitioning the numbers before formal column to show the exchange.</p> $\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$

Y4-6

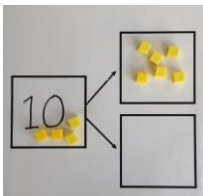
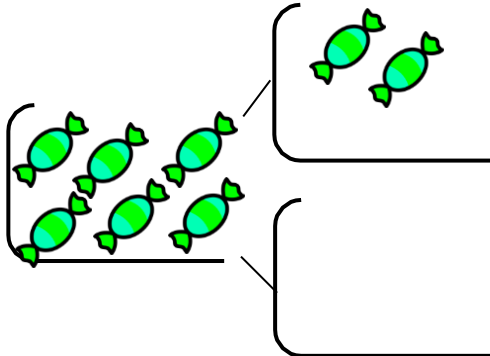
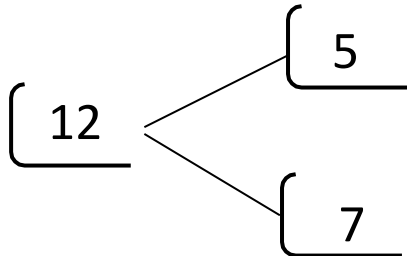
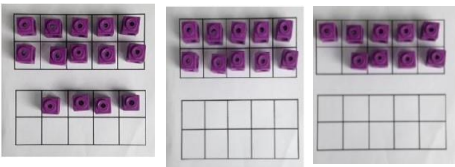
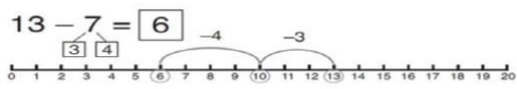
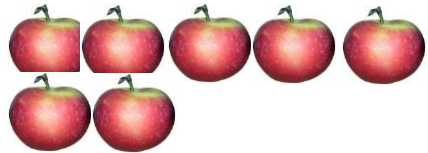


ADDITION +

Objective & Strategy	Concrete	Pictorial	Abstract									
Y4—add numbers with up to 4 digits	<p>Children continue to use dienes or pv counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand.</p> <table border="1"><thead><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></tbody></table>	Hundreds	Tens	Ones							 <p>Draw representations using pv grid.</p>	 <p>Continue from previous work to carry hundreds as well as tens.</p> <p>Relate to money and measures.</p>
Hundreds	Tens	Ones										
												
												
Y5—add numbers with more than 4 digits. Add decimals with 2 decimal places, including money.	<p>As year 4</p> <table border="1"><thead><tr><th>tens</th><th>ones</th><th>tenths</th><th>hundredths</th></tr></thead><tbody><tr><td></td><td></td><td></td><td></td></tr></tbody></table> <p>Introduce decimal place value counters and model exchange for addition.</p>	tens	ones	tenths	hundredths						 	
tens	ones	tenths	hundredths									
												
Y6—add several numbers of increasing complexity Including adding money, measure and decimals with different numbers of decimal points.	As Y5	As Y5	  <p>Insert zeros for place holders.</p>									

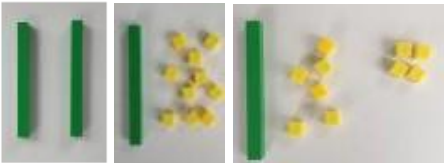
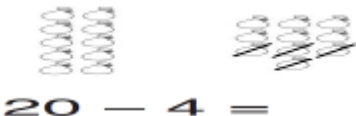

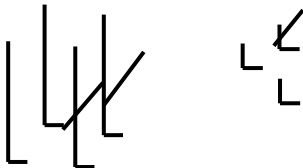
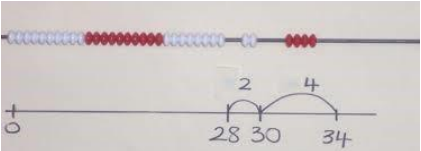
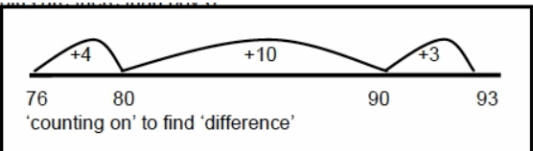
Y1 SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract
Taking away ones.	<p>Use physical objects, counters, cubes etc to show how objects can be taken away.</p>  <p>$4 - 2 = 2$</p> <p>$6 - 4 = 2$</p>	 <p>$15 - 3 = 12$</p> <p>Cross out drawn objects to show what has been taken away.</p>	<p>$7 - 4 = 3$</p> <p>$16 - 9 = 7$</p>
Counting back	 <p>Move objects away from the group, counting backwards.</p> <p>Move the beads along the bead string as you count backwards.</p>	 <p>$5 - 3 = 2$</p> <p>Count back in ones using a number line.</p>	<p>Put 13 in your head, count back 4. What number are you at?</p>
Find the Difference	<p>Compare objects and amounts</p>  <p>'Seven is 3 more than four'</p> <p>'I am 2 years older than my sister'</p> <p>5 Pencils</p> <p>3 Erasers</p> <p>?</p> <p>Lay objects to represent bar model.</p>	<p>Count on using a number line to find the difference.</p>  <p>+6</p>	<p>Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister.?</p>

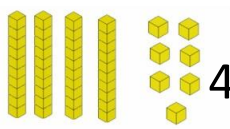
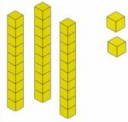
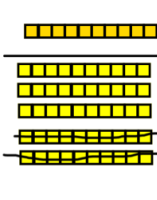
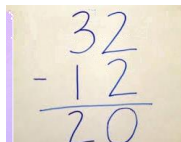













Y1 SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract
Represent and use number bonds and related subtraction facts within 20 Part Part Whole model	 <p>Link to addition. Use PPW model to model the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what is the other part?</p> $10 - 6 = 4$	 <p>Use pictorial representations to show the part.</p>	<p>Move to using numbers within the part whole model.</p> 
Make 10	<p>14—9</p>  <p>Make 14 on the ten frame. Take 4 away to make ten, then take one more away so that you have taken 5.</p>	<p>13—7</p>  <p>Jump back 3 first, then another 4. Use ten as the stopping point.</p>	<p>16—8</p> <p>How many do we take off first to get to 10? How many left to take off?</p>
Bar model	 $5 - 2 = 3$		 $10 = 8 + 2$ $10 = 2 + 8$ $10 - 2 = 8$ $10 - 8 = 2$

Y2 SUBTRACTION -

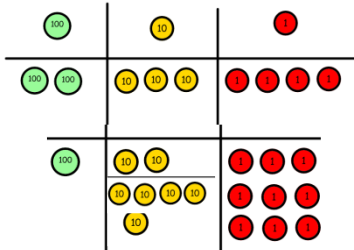
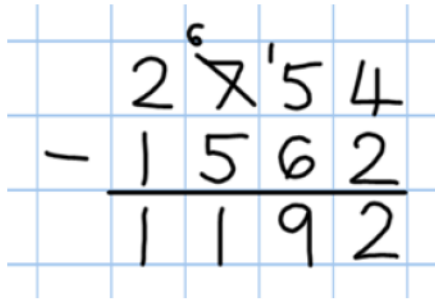
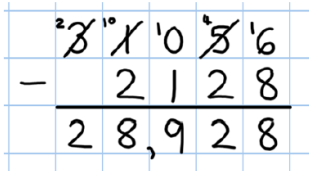
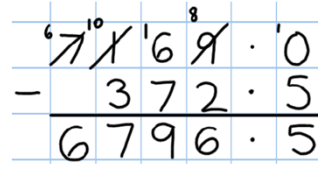
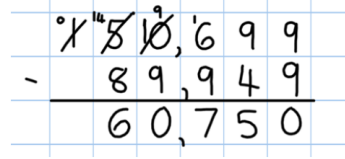
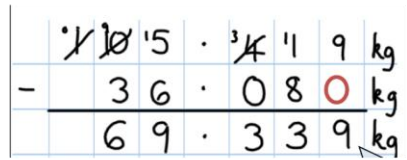
Objective & Strategy	Concrete	Pictorial	Abstract
Regroup a ten into ten ones	 <p>Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'</p>	 $20 - 4 =$	$20 - 4 = 16$
Partitioning to subtract without regrouping. <i>'Friendly numbers'</i>	$34 - 13 = 21$  <p>Use Dienes to show how to partition the number when subtracting without regrouping.</p>	<p>Children draw representations of Dienes and cross off.</p>  $43 - 21 = 22$	$43 - 21 = 22$
Make ten strategy <i>Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.</i>	 $34 - 28$ <p>Use a bead bar or bead strings to model counting to next ten and the rest.</p>	 <p>Use a number line to count on to next ten and then the rest.</p>	$93 - 76 = 17$

Y3 SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract																														
Column subtraction without regrouping (friendly numbers)	<div>$47-32$</div> <div> —</div> <p>Use base 10 or Numicon to model</p>	<div></div> <p>Draw representations to support understanding</p>	<div>$47-24=23$ $\begin{array}{r} 40+7 \\ -20+4 \\ \hline 20+3 \end{array}$</div> <p>Intermediate step may be needed to lead to clear subtraction understanding.</p> <div></div>																														
Column subtraction with regrouping	<div><table><tr><th>Tens</th><th>Units</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table></div> <p>Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase ‘take and make’ for exchange.</p>	Tens	Units					<div>$\begin{array}{r} 45 \\ -29 \\ \hline 16 \end{array}$<div>Tens Ones</div>$\begin{array}{l} 10 + 6 = 16 \\ 10 - 10 = 0 \end{array}$</div> <p>Children may draw base ten or PV counters and cross off.</p>	<div>$836-254=582$<table><tr><th>H</th><th>T</th><th>U</th></tr><tr><td>800</td><td>30</td><td>6</td></tr><tr><td>- 200</td><td>50</td><td>4</td></tr><tr><td>500</td><td>80</td><td>2</td></tr></table></div> <p>Begin by partitioning into pv columns</p> <div>$728-582=146$<table><tr><th>H</th><th>T</th><th>U</th></tr><tr><td>700</td><td>20</td><td>8</td></tr><tr><td>- 500</td><td>80</td><td>2</td></tr><tr><td>200</td><td>40</td><td>6</td></tr></table></div> <p>Then move to formal method.</p>	H	T	U	800	30	6	- 200	50	4	500	80	2	H	T	U	700	20	8	- 500	80	2	200	40	6
Tens	Units																																
																																	
																																	
H	T	U																															
800	30	6																															
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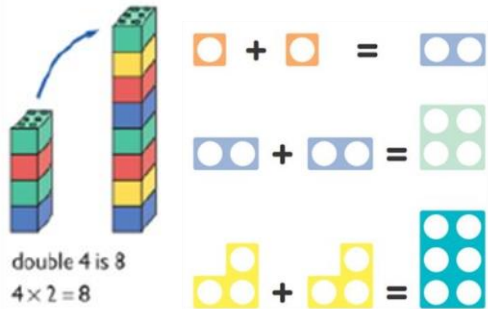
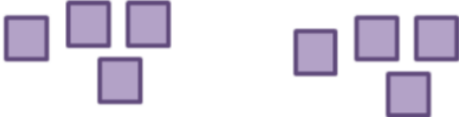
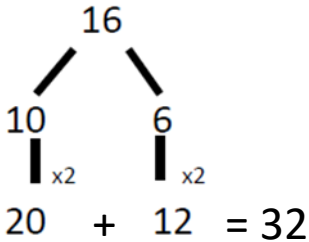
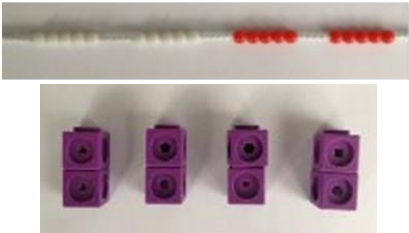
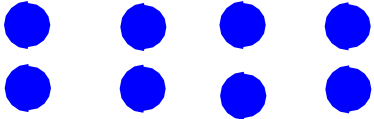
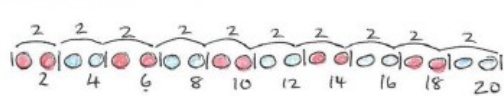
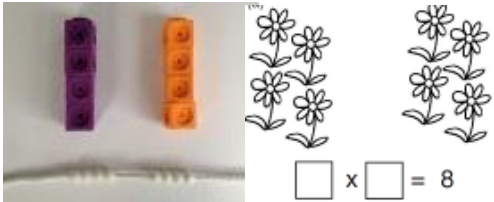

Y4-6

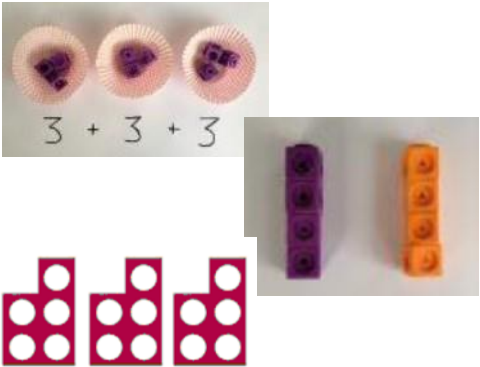
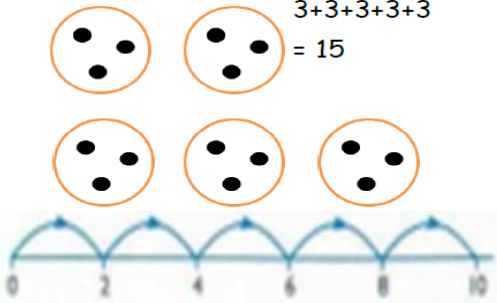

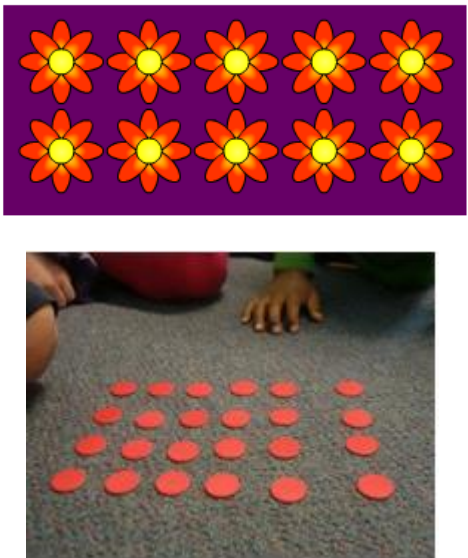
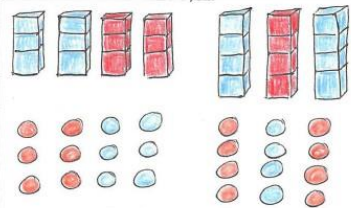
SUBTRACTION -

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Subtracting tens and ones</p> <p>Year 4 subtract with up to 4 digits.</p> <p><i>Introduce decimal subtraction through context of money</i></p>	<p>234 - 179</p>  <p>Model process of exchange using Numicon, base ten and then move to PV counters.</p>	<p>Children to draw pv counters and show their exchange—see Y3</p>	 <p>Use the phrase 'take and make' for exchange</p>
<p>Year 5- Subtract with at least 4 digits, including money and measures.</p> <p><i>Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal</i></p>	<p>As Year 4</p>	<p>Children to draw pv counters and show their exchange—see Y3</p>	 <p>Use zeros for place-holders.</p> 
<p>Year 6—Subtract with increasingly large and more complex numbers and decimal values.</p>			 

Y1

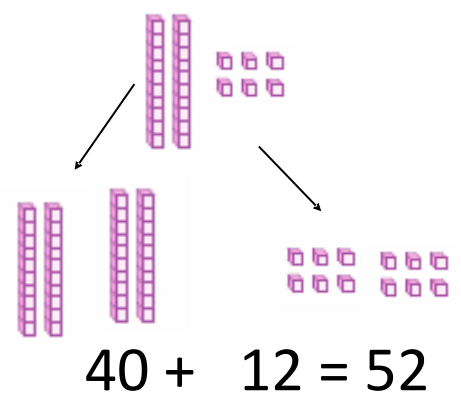
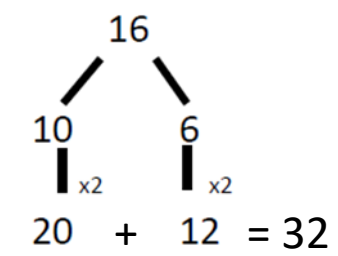


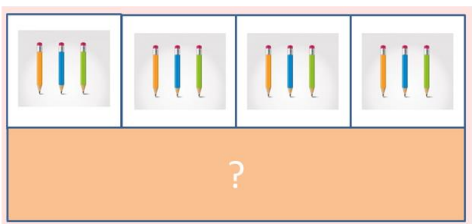
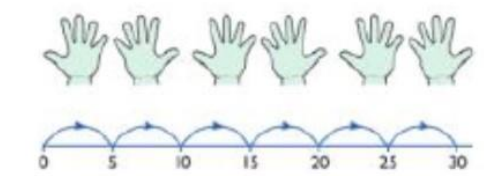
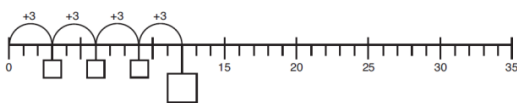
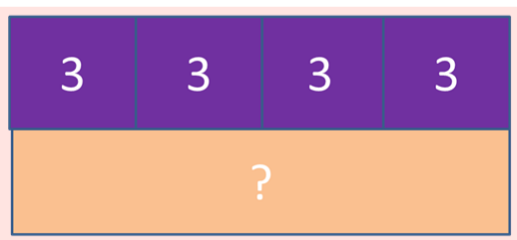
MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
Doubling	<p>Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling</p>  <p>double 4 is 8 $4 \times 2 = 8$</p>	<p>Draw pictures to show how to double numbers</p> <p>Double 4 is 8</p> 	<p>Partition a number and then double each part before recombining it back together.</p>  <p>16 10 and 6 $10 \times 2 = 20$ $6 \times 2 = 12$ $20 + 12 = 32$</p>
Counting in multiples	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	 <p>Children make representations to show counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>
Making equal groups and counting the total	 <p>$\square \times \square = 8$</p> <p>Use manipulatives to create equal groups.</p>	<p>Draw  to show $2 \times 3 = 6$</p> <p>Draw and make representations</p>	<p>$2 \times 4 = 8$</p>

Objective & Strategy	Concrete	Pictorial	Abstract
Repeated addition	 <p>Use different objects to add equal groups</p>	<p>Use pictorial including number lines to solve problem There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>  $3 + 3 + 3 + 3 + 3 = 15$	<p>Write addition sentences to describe objects and pictures.</p>  $2 + 2 + 2 + 2 + 2 = 10$
Understanding arrays	<p>Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.</p> 	<p>Draw representations of arrays to show understanding</p> 	$3 \times 2 = 6$ $2 \times 5 = 10$



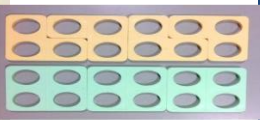

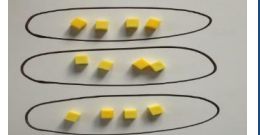
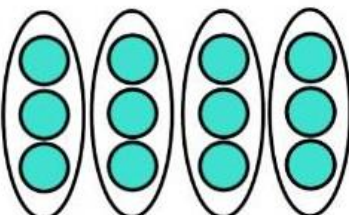
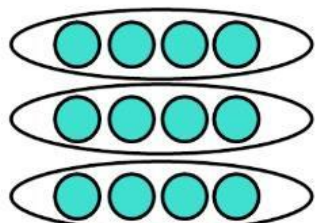


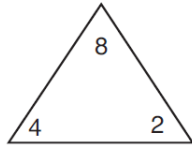
Y2

MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
Doubling	<p>Model doubling using dienes and PV counters.</p>  $40 + 12 = 52$	<p>Draw pictures and representations to show how to double numbers</p>	<p>Partition a number and then double each part before recombining it back together.</p>  $16 \begin{matrix} \swarrow & \searrow \\ 10 & 6 \end{matrix} \begin{matrix} \downarrow \times 2 & \downarrow \times 2 \\ 20 & 12 \end{matrix} \quad 20 + 12 = 32$
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models.</p>  $5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$  	<p>Number lines, counting sticks and bar models should be used to show representation of counting in multiples.</p>   	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>0, 2, 4, 6, 8, 10</p> <p>0, 3, 6, 9, 12, 15</p> <p>0, 5, 10, 15, 20, 25, 30</p> $4 \times 3 = \square$

Y2

MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Multiplication is commutative</p>	<p>Create arrays using counters and cubes and Numicon.</p>    <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p>  	<p>Use representations of arrays to show different calculations and explore commutativity.</p>  	<p>$12 = 3 \times 4$</p> <p>$12 = 4 \times 3$</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p>$5 + 5 + 5 = 15$</p> <p>$3 + 3 + 3 + 3 + 3 = 15$</p> <p>$5 \times 3 = 15$</p> <p>$3 \times 5 = 15$</p>
<p>Using the Inverse</p> <p><i>This should be taught alongside division, so pupils learn how they work alongside each other.</i></p>		 <p>$\square \times \square = \square$</p> <p>$\square \times \square = \square$</p> <p>$\square \div \square = \square$</p> <p>$\square \div \square = \square$</p>	<p>$2 \times 4 = 8$</p> <p>$4 \times 2 = 8$</p> <p>$8 \div 2 = 4$</p> <p>$8 \div 4 = 2$</p> <p>$8 = 2 \times 4$</p> <p>$8 = 4 \times 2$</p> <p>$2 = 8 \div 4$</p> <p>$4 = 8 \div 2$</p> <p>Show all 8 related fact family sentences.</p>

Y3

MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
Grid method	<p>Show the links with arrays to first introduce the grid method.</p> <div><div><div><div>x</div><div>10</div><div>3</div></div><div><div>4</div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></di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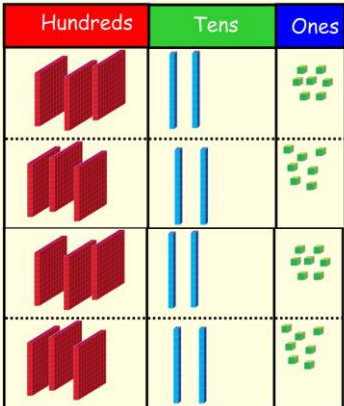
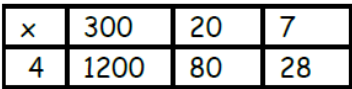

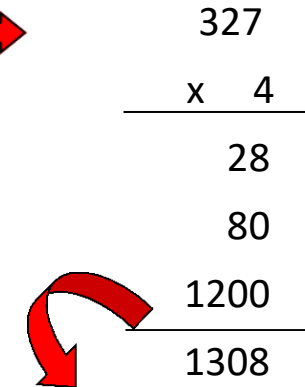
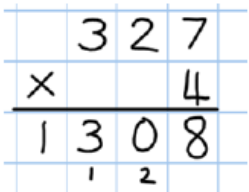
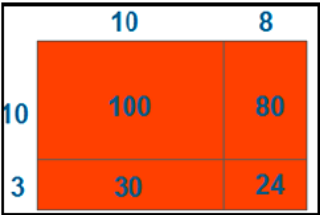

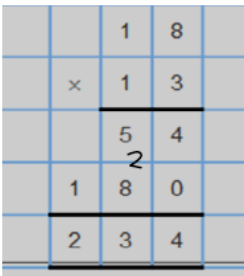
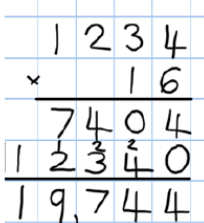
Y4

MULTIPLICATION X

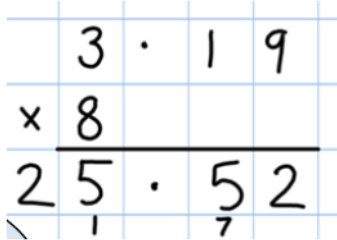
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Grid method recap from year 3 for 2 digits x 1 digit</p> <p>Move to multiplying 3 digit numbers by 1 digit. (year 4 expectation)</p>	<p>Use place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows</p> <div><div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div><div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div><div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div><div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div></div> <p>Calculations 4 x 126</p> <p>Fill each row with 126</p> <div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div> <div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div> <div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div> <div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div><div><div>100</div><div>10</div><div>1</div></div></div> <p>Add up each column, starting with the ones making any exchanges needed</p>	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p> <div><div><div>24</div><div>x</div><div>3</div><div>=</div><div>72</div></div><div><div><div>3</div><div>x</div><div>20</div><div>=</div><div>60</div></div><div><div><div>3</div><div>x</div><div>4</div><div>=</div><div>12</div></div><div><div><div>60</div><div>+</div><div>12</div><div>=</div><div>72</div></div></div></div></div></div>	<p>Start with multiplying by one digit numbers and showing the clear addition alongside the grid.</p> <div><div><div><div>x</div><div>30</div><div>5</div></div><div><div>7</div><div>210</div><div>35</div></div></div><div><div>210</div><div>+</div><div>35</div><div>=</div><div>245</div></div></div>
<p>Column multiplication</p>	<p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. 321 x 2 = 642</p> <div><div><div><div>Hundreds</div><div>Tens</div><div>Ones</div></div><div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div><div><div><div></div><div></div><div></div></div></div></div></div><div><div>It is important at this stage that they always multiply the ones first.</div></div><p>The corresponding long multiplication is modelled alongside</p></div></div></div></div></div></div></div></div></div>	<div><div><div><div>x</div><div>300</div><div>20</div><div>7</div></div><div><div>4</div><div>1200</div><div>80</div><div>28</div></div></div><div><div>Children can represent their work with place value counters in a way that they understand.</div><div>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</div><div><div><div>59</div><div>59</div><div>59</div><div>59</div><div>59</div><div>59</div><div>59</div><div>59</div></div><div><div><div>8 x 59</div><div>= 8 x 60 - 8</div><div>8 x 6 = 48</div><div>8 x 60 = 480</div><div>480 - 8 = 472</div></div></div></div><p>Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.</p></div></div>	<div><div><div>327</div><div>x</div><div>4</div></div><div><div>28</div><div>80</div><div>1200</div><div>1308</div></div><div><div><div><div>x</div><div>327</div><div>4</div></div><div><div>1308</div></div></div><div><div>This may lead to a compact method.</div></div></div></div>


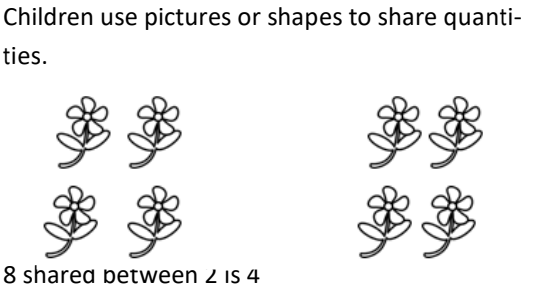
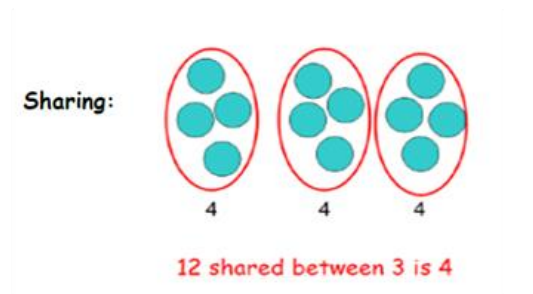
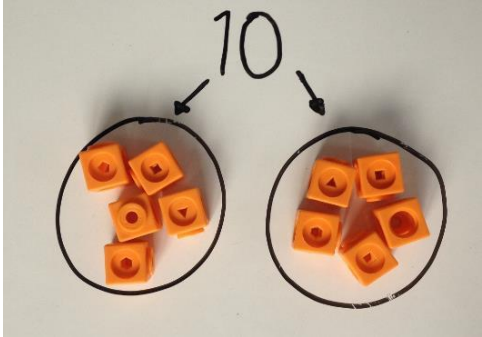
Y5-6

MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Column Multiplication for 3 and 4 digits x 1 digit.</p>	 <p>It is important at this stage that they always multiply the ones first.</p> <p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$</p>	 	  <p>This will lead to a compact method.</p>
<p>Column multiplication</p>	<p>Manipulatives may still be used with the corresponding long multiplication modelled alongside.</p>	 	 <p>18 x 3 on the first row (8 x 3 = 24, carrying the 2 for 20, then 1 x 3)</p> <p>18 x 10 on the 2nd row. Show multiplying by 10 by putting zero in units first</p>  <p>Continue to use bar modelling to support problem solving</p>

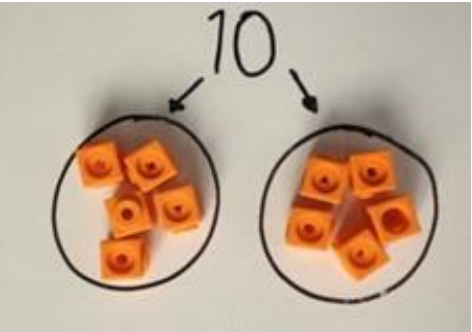
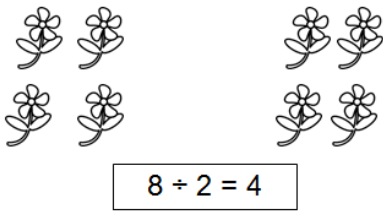
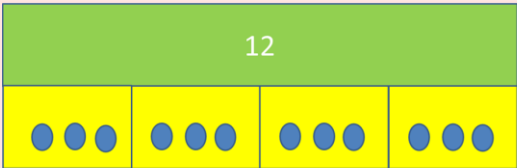
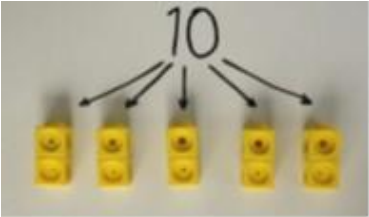

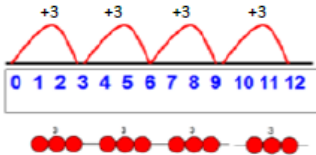
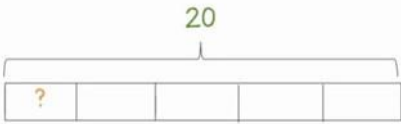
Y6 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
Multiplying decimals up to 2 decimal places by a single digit.			<p>Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.</p> 

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Division as sharing</p> <p>Use Gordon ITPs for modelling</p>		<p>Children use pictures or shapes to share quantities.</p>  <p>8 shared between 2 is 4</p> <p>Sharing:</p>  <p>12 shared between 3 is 4</p>	<p>12 shared between 3 is 4</p>
	 <p>I have 10 cubes, can you share them equally in 2 groups?</p>		

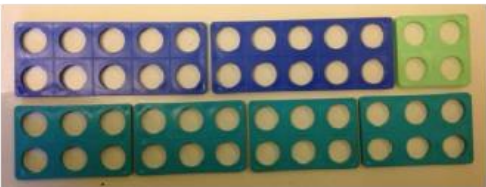


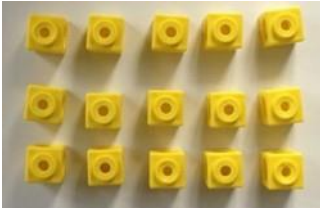
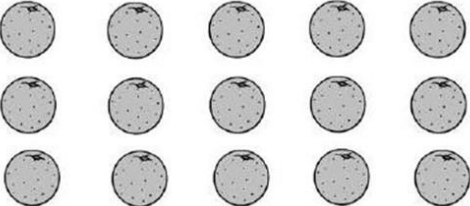
Y2

DIVISION ÷

Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing	 <p>I have 10 cubes, can you share them equally in 2 groups?</p>	<p>Children use pictures or shapes to share quantities.</p>  <p>$8 \div 2 = 4$</p> <p>Children use bar modelling to show and support understanding.</p>  <p>$12 \div 4 = 3$</p>	$12 \div 3 = 4$
Division as grouping	<p>Divide quantities into equal groups.</p> <p>Use cubes, counters, objects or place value counters to aid understanding.</p>  	<p>Use number lines for grouping</p>  <p>$12 \div 3 = 4$</p> <p>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p>	$28 \div 7 = 4$ <p>Divide 28 into 7 groups. How many are in each group?</p>

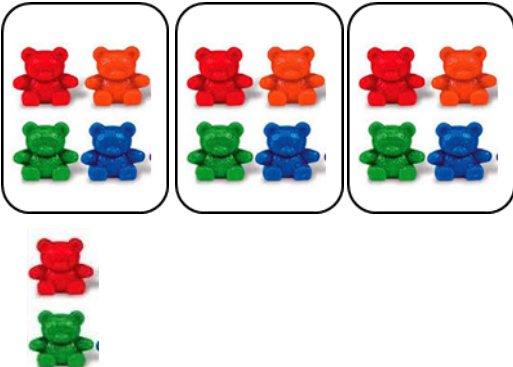

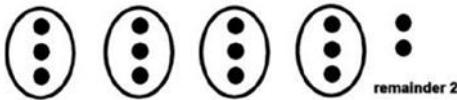
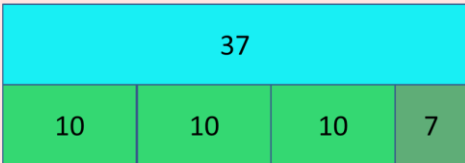
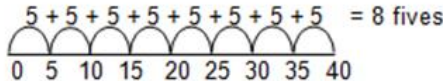
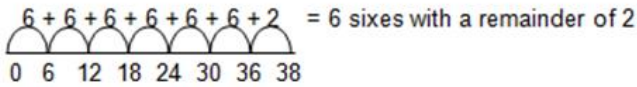
Y3

DIVISION

Objective & Strategy	Concrete	Pictorial	Abstract
Division as grouping	<p>Use cubes, counters, objects or place value counters to aid understanding.</p>  <p>24 divided into groups of 6 = 4</p> $96 \div 3 = 32$ 	<p>Continue to use bar modelling to aid solving division problems.</p>  $20 \div 5 = ?$ $5 \times ? = 20$	<p>How many groups of 6 in 24?</p> $24 \div 6 = 4$
Division with arrays	 <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg $15 \div 3 = 5$ $5 \times 3 = 15$</p> <p>$15 \div 5 = 3$ $3 \times 5 = 15$</p>	<p>Draw an array and use lines to split the array into groups to make multiplication and division sentences</p> 	<p>Find the inverse of multiplication and division sentences by creating eight linking number sentences.</p> $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$ $28 = 7 \times 4$ $28 = 4 \times 7$ $4 = 28 \div 7$ $7 = 28 \div 4$

Y3

DIVISION ÷

Objective & Strategy	Concrete	Pictorial	Abstract
Division with remainders.	<p>$14 \div 3 =$</p> <p>Divide objects between groups and see how much is left over</p> 	<p>Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.</p>  <p>Draw dots and group them to divide an amount and clearly show a remainder.</p>  <p>Use bar models to show division with remainders.</p>  <p>Example without remainder: $40 \div 5$ Ask "How many 5s in 40?"  $5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 8 \text{ fives}$</p> <p>Example with remainder: $38 \div 6$  $6 + 6 + 6 + 6 + 6 + 6 + 2 = 6 \text{ sixes with a remainder of } 2$</p> <p>For larger numbers, when it becomes inefficient to count in single multiples, bigger jumps can be recorded using known facts.</p>	<p>Complete written divisions and show the remainder using r.</p> <p>$29 \div 8 = 3 \text{ REMAINDER } 5$</p> <p> \uparrow \uparrow \uparrow \uparrow dividend divisor quotient remainder </p>



Objective & Strategy	Concrete	Pictorial	Abstract						
<p>Divide at least 3 digit numbers by 1 digit.</p> <p>Short Division</p>	<p>$96 \div 3$</p> <table><thead><tr><th></th><th>Tens</th><th>Units</th></tr></thead><tbody><tr><td>3</td><td>3</td><td>2</td></tr></tbody></table> <p>Use place value counters to divide using the bus stop method alongside</p> <p>42 \div 3 =</p> <p>Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.</p> <p>We exchange this ten for ten ones and then share the ones equally among the groups.</p> <p>We look how much in 1 group so the answer is 14.</p>		Tens	Units	3	3	2	<p>Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.</p> <p>Encourage them to move towards counting in multiples to divide more efficiently.</p>	<p>Begin with divisions that divide equally with no remainder.</p> $\begin{array}{r} 218 \\ 3 \overline{) 654} \end{array}$ <p>Move onto divisions with a remainder.</p> $\begin{array}{r} 86 \text{ r } 2 \\ 3 \overline{) 432} \end{array}$ <p>Finally move into decimal places to divide the total accurately.</p> $\begin{array}{r} 14.6 \\ 35 \overline{) 511.0} \end{array}$ $\begin{array}{r} 0663 \text{ r } 5 \\ 8 \overline{) 5309} \end{array}$
	Tens	Units							
3	3	2							

Long Division

Step 1—a remainder in the ones

$$\begin{array}{r} \text{h t o} \\ 0 \ 4 \ 1 \ \text{R}1 \\ 4 \overline{) \ 1 \ 6 \ 5} \end{array}$$

4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).

4 goes into 16 four times.

4 goes into 5 once, leaving a remainder of 1.

$$\begin{array}{r} \text{th h t o} \\ 0 \ 4 \ 0 \ 0 \ \text{R}7 \\ 8 \overline{) \ 3 \ 2 \ 0 \ 7} \end{array}$$

8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).

8 goes into 32 four times ($3,200 \div 8 = 400$)

8 goes into 0 zero times (tens).

8 goes into 7 zero times, and leaves a remainder of 7.

Y6

DIVISION



Objective & Strategy	Concrete	Pictorial	Abstract
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Recording remainder as a whole, decimal and fraction

$$\begin{array}{r} 858 \text{ r } 2 \\ 3 \overline{) 2576} \end{array}$$

$$\begin{array}{r} 812.125 \\ 8 \overline{) 6497.000} \end{array}$$

Answer: $858 \frac{2}{3}$

$$\begin{array}{r} 186 \\ 3 \overline{) 558} \end{array} \quad \begin{array}{r} 31 \\ 6 \overline{) 186} \end{array}$$

- 1: Identify a pair of factors for the divisor e.g. one of the factors.
 2: Divide by
 3: Divide the answer by the other factor.

Answer: $558 \div 18 = 31$

$$\begin{array}{r} 4 \\ \cancel{5} 58 \\ - 360 \text{ (20 x 18)} \\ \hline 198 \\ - 180 \text{ (10 x 18)} \\ \hline 18 \\ - 18 \text{ (1 x 18)} \\ \hline 0 \end{array}$$

Answer: $558 \div 18 = 31$

$$\begin{array}{l} 2544 \div 12 = \boxed{} \\ 12 = 6 \times 2 \\ \begin{array}{r} 1272 \\ 2 \overline{) 2544} \\ \underline{212} \\ 432 \\ \underline{420} \\ 120 \\ \underline{120} \\ 0 \end{array} \\ 6 \overline{) 1272} \\ \underline{12} \\ 72 \\ \underline{72} \\ 0 \end{array}$$

$18 = 3 \times 6$

$$\begin{array}{r} 212 \\ 12 \overline{) 2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$$

Use these related number facts to divide.

- 12×1
- 24×2
- 48×4
- 96×8

